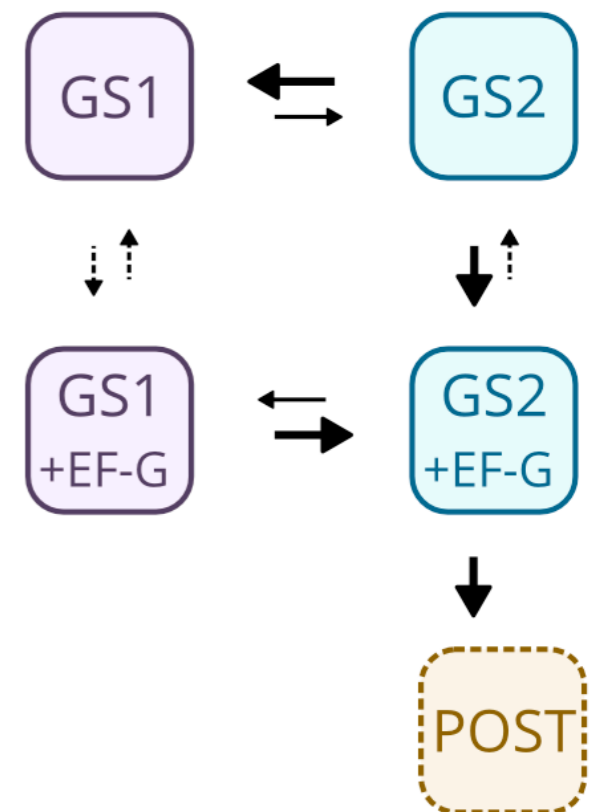
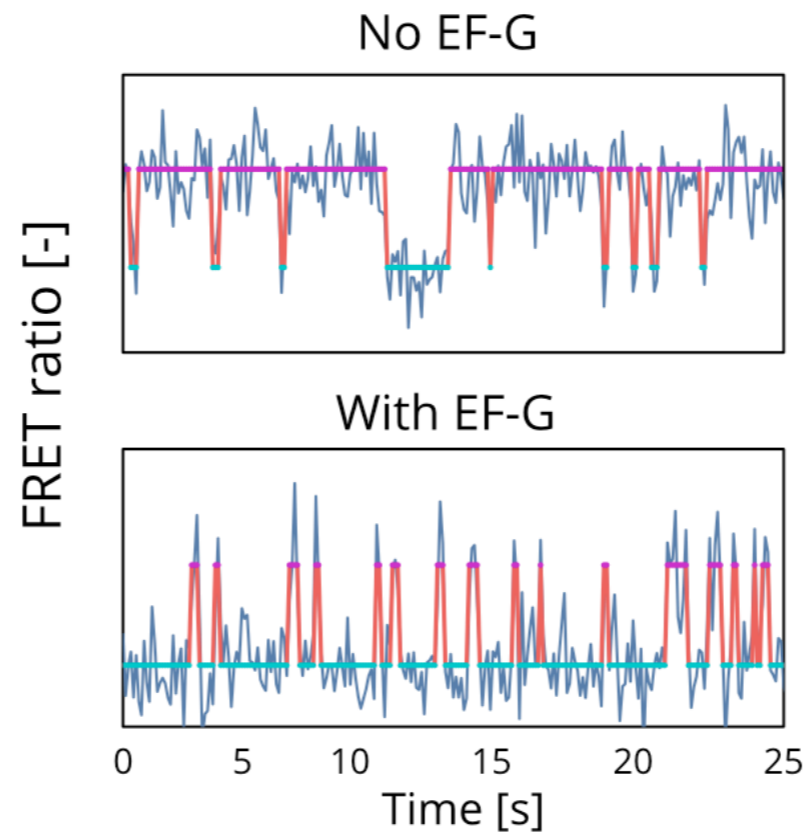
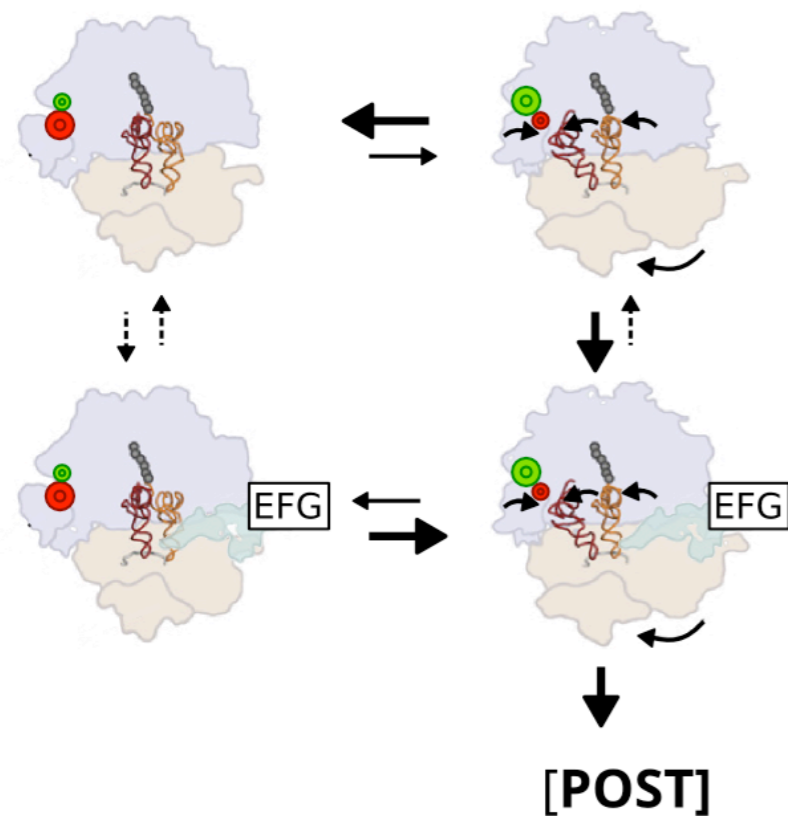
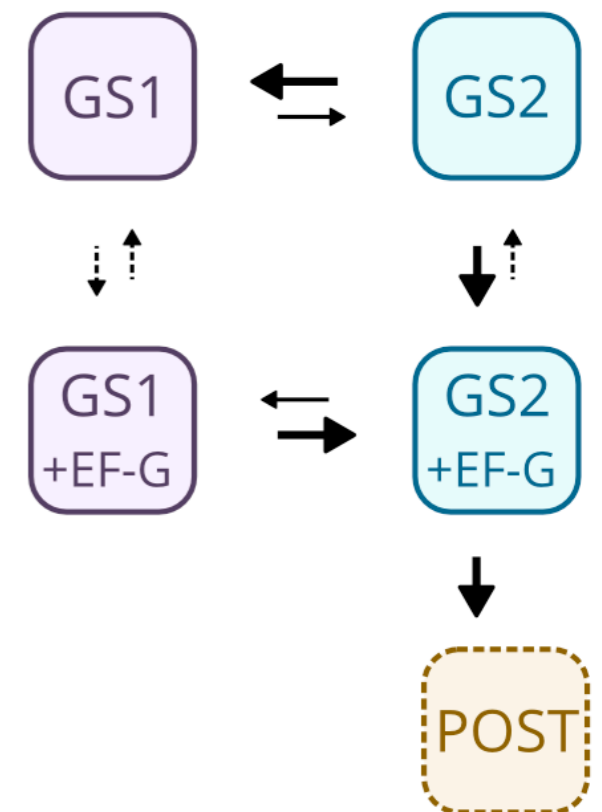
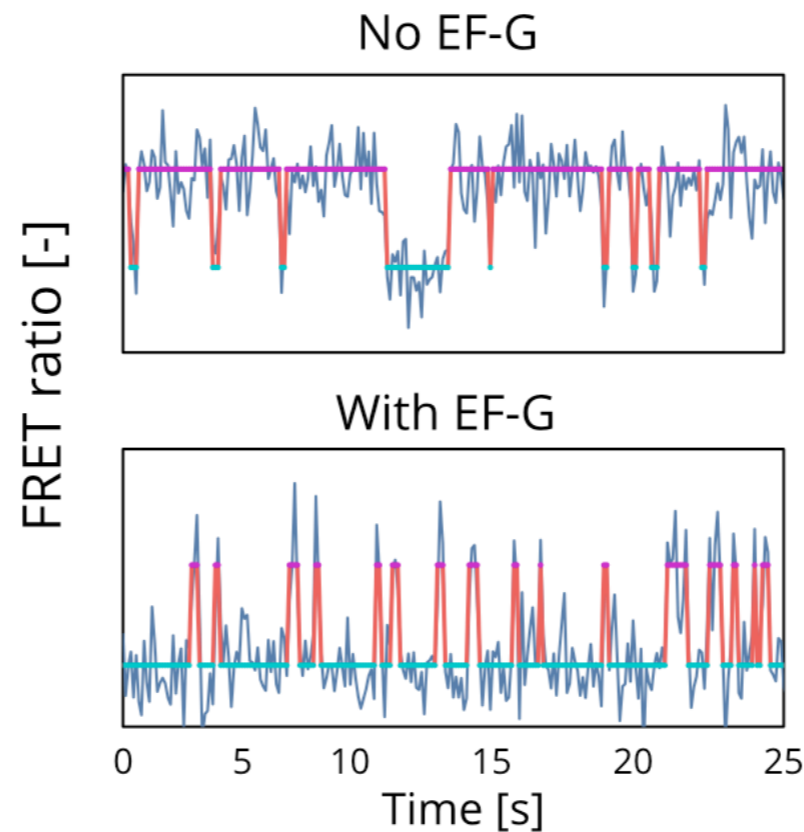
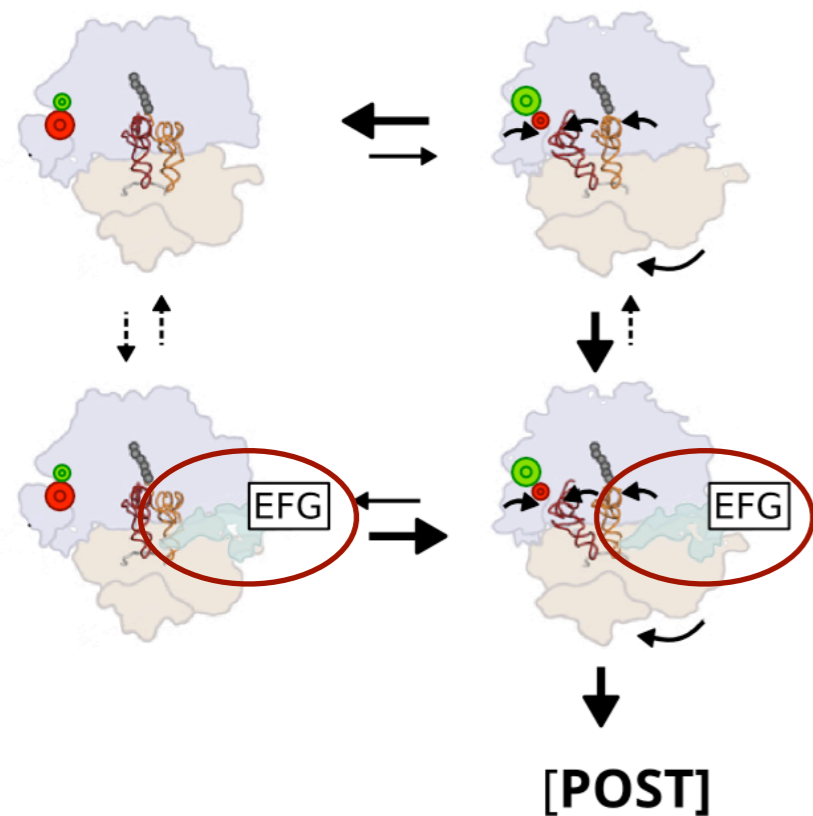


# Learning Kinetic Models from Single-Molecule Experiments



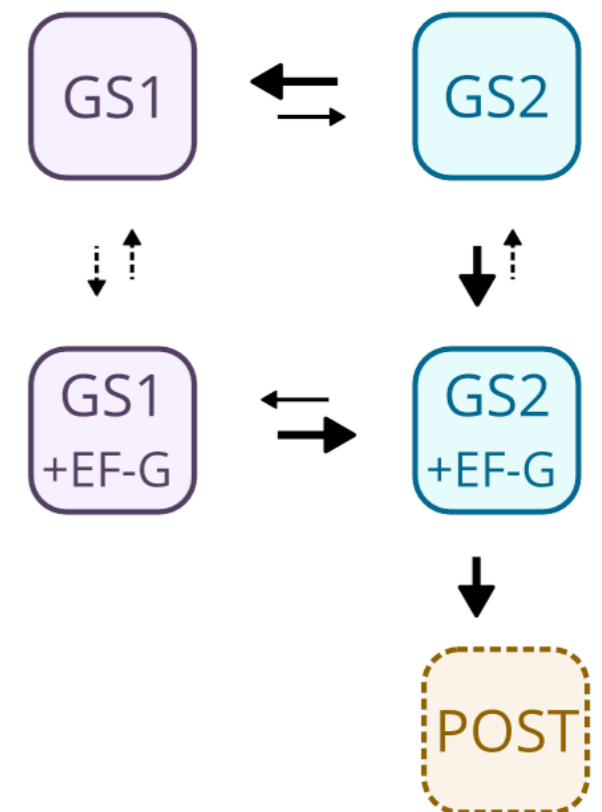
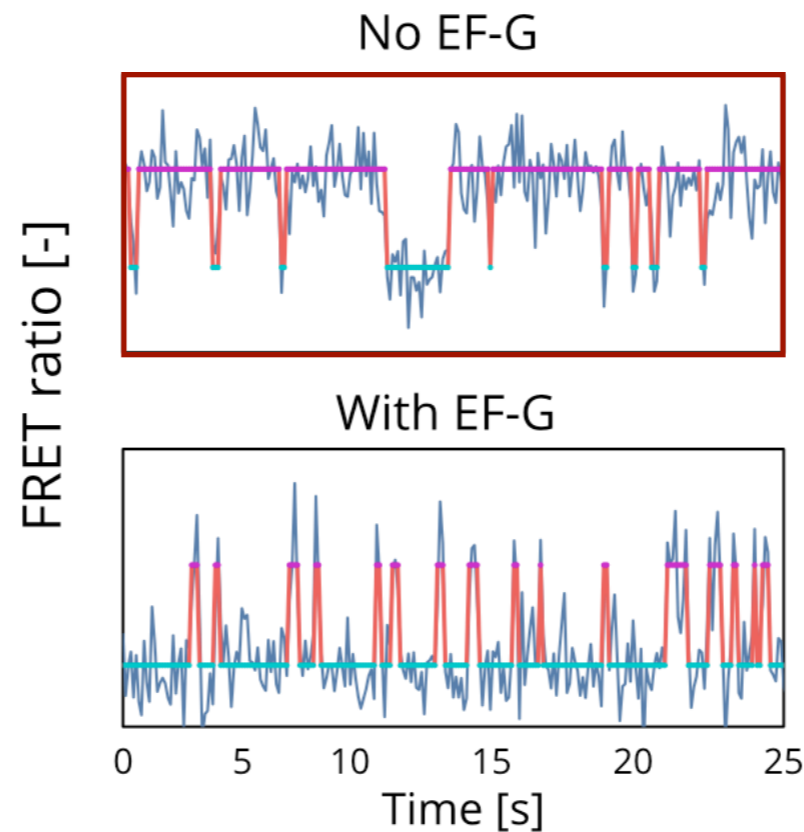
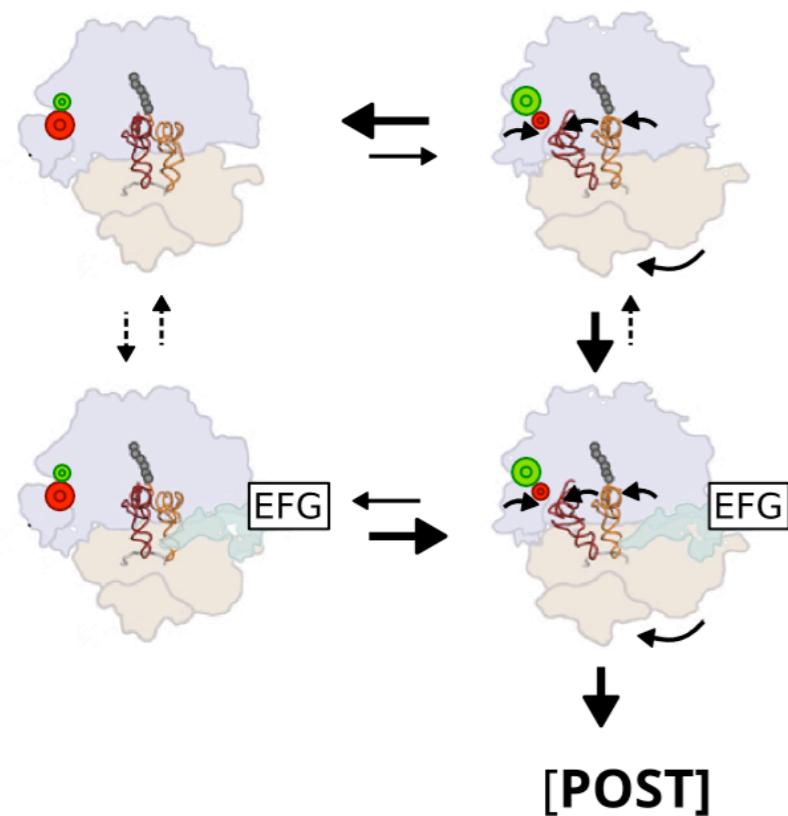
Single-molecule FRET studies of the Ribosome  
Ruben Gonzalez (Columbia)

# Learning Kinetic Models from Single-Molecule Experiments



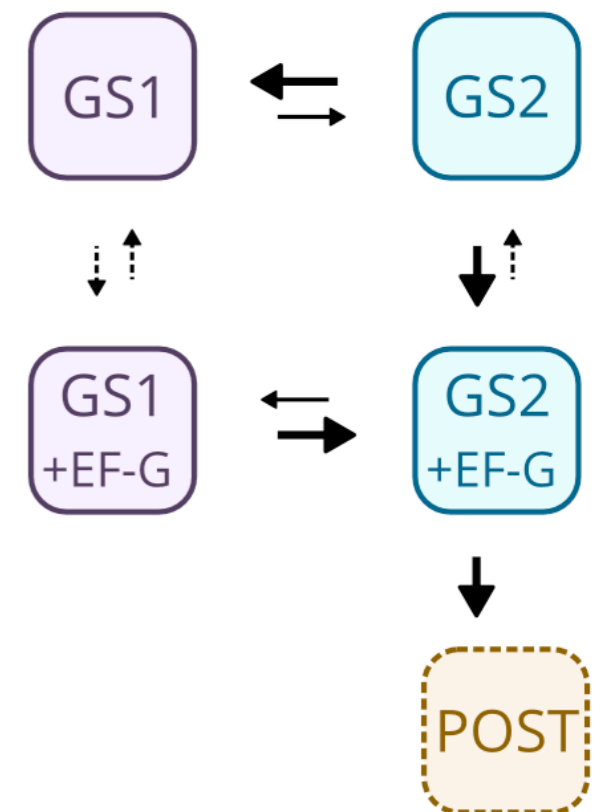
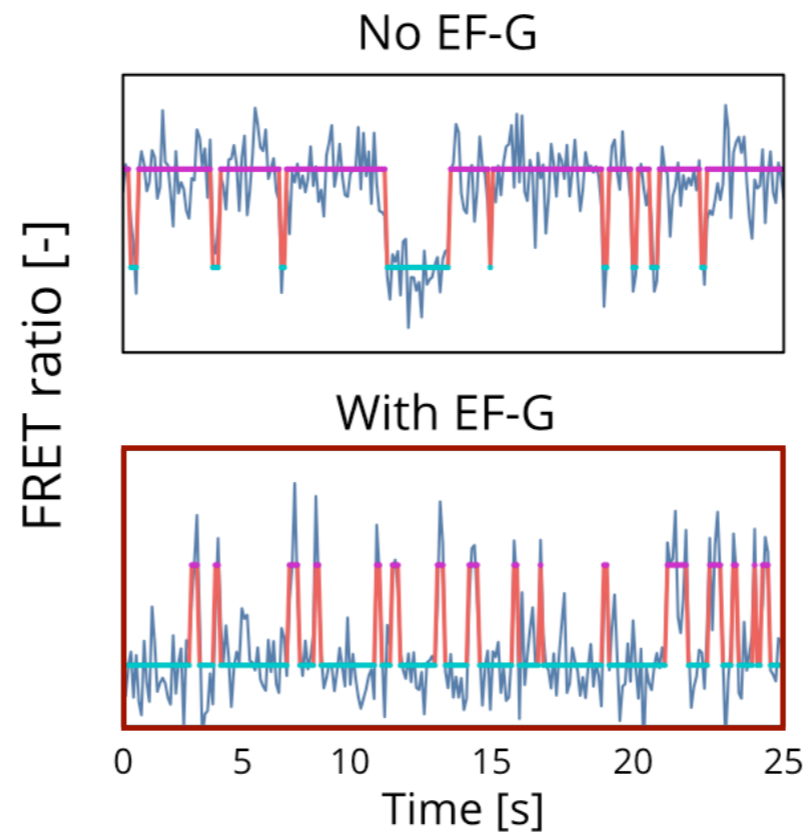
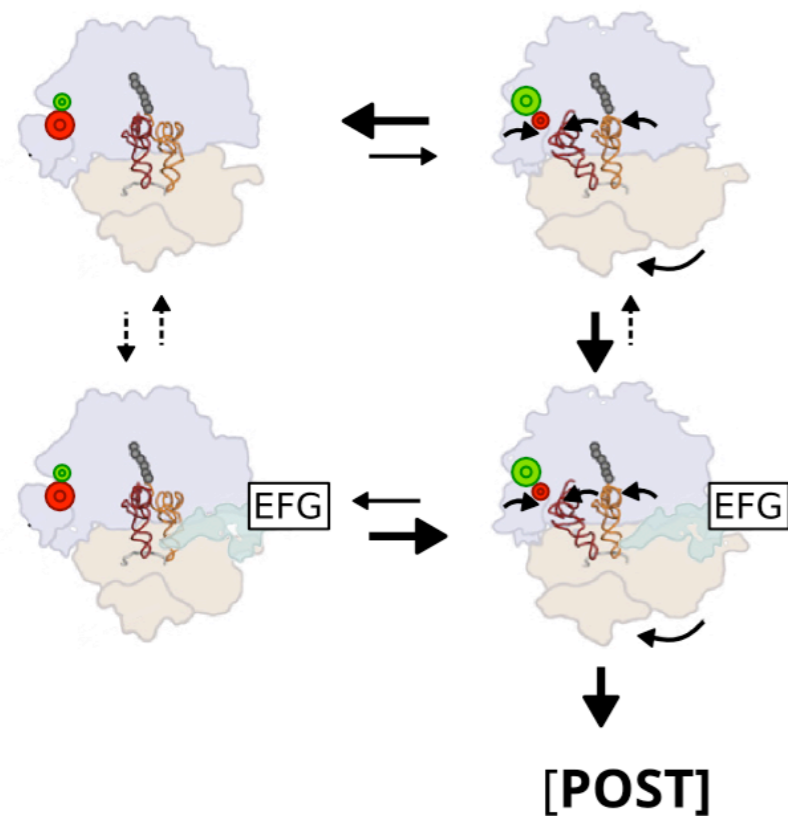
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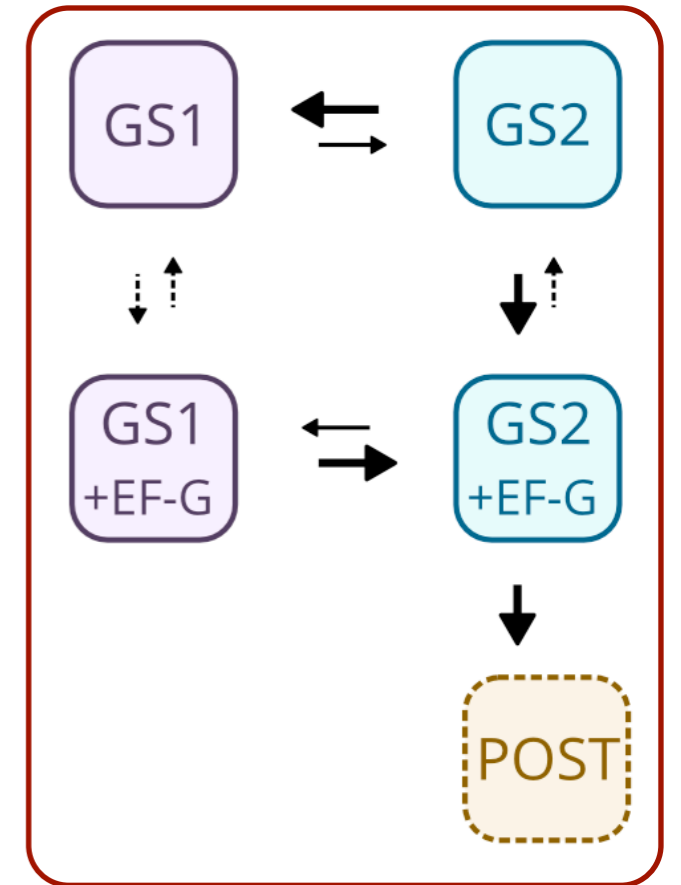
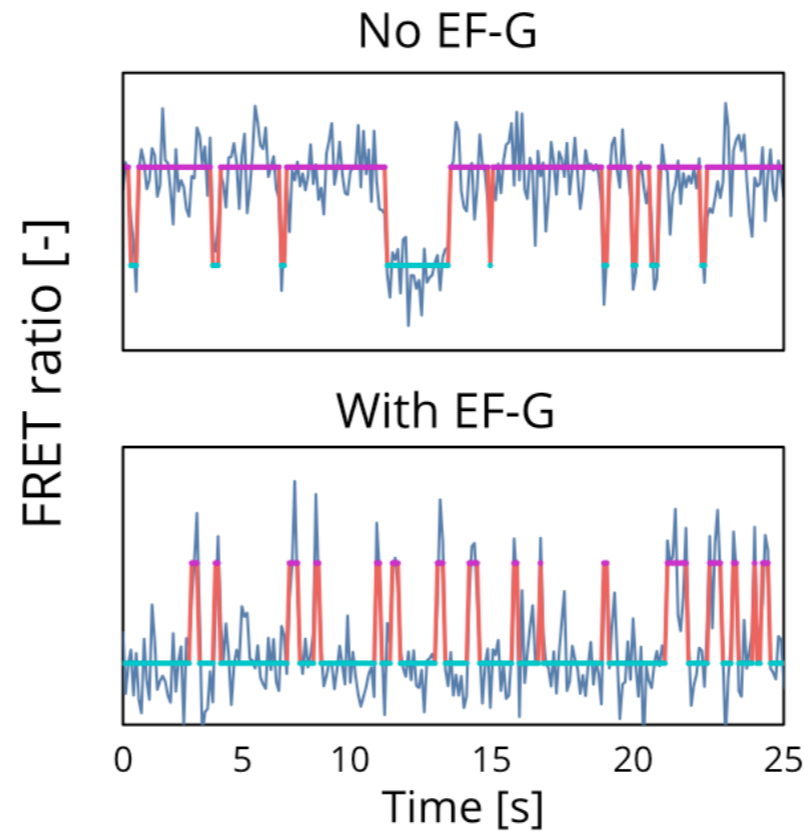
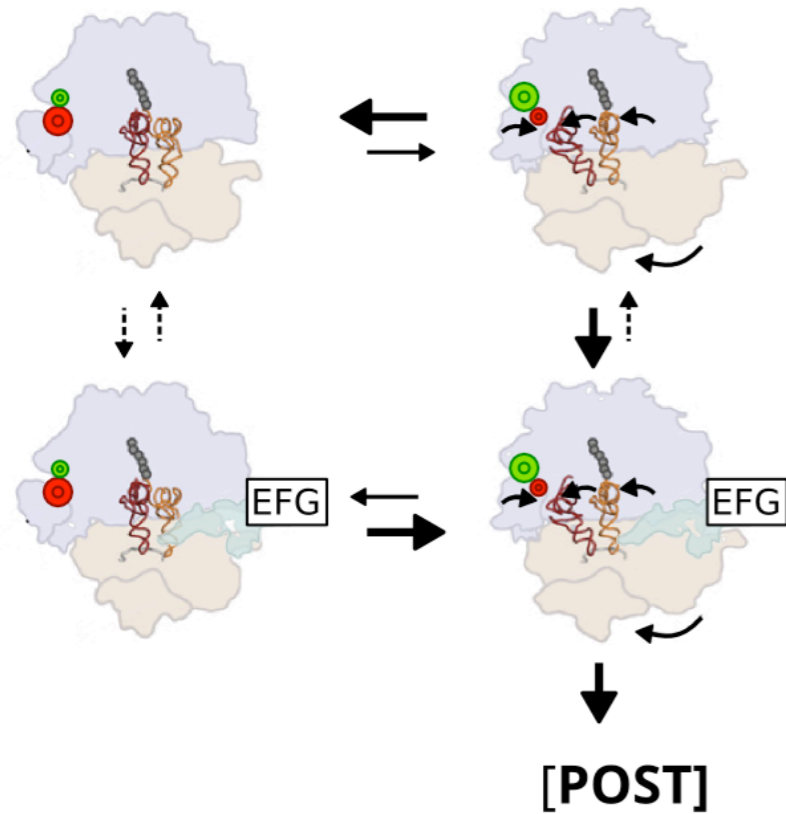
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# Learning Kinetic Models from Single-Molecule Experiments



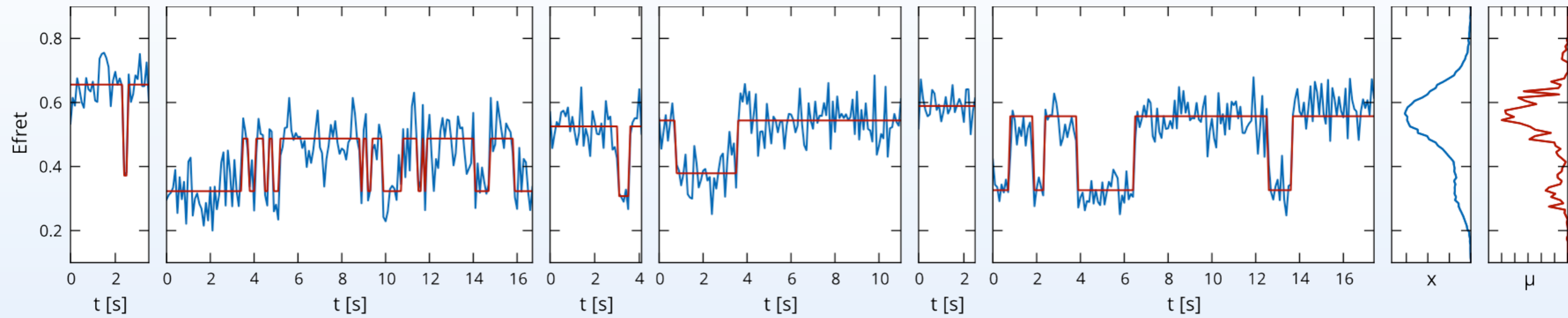
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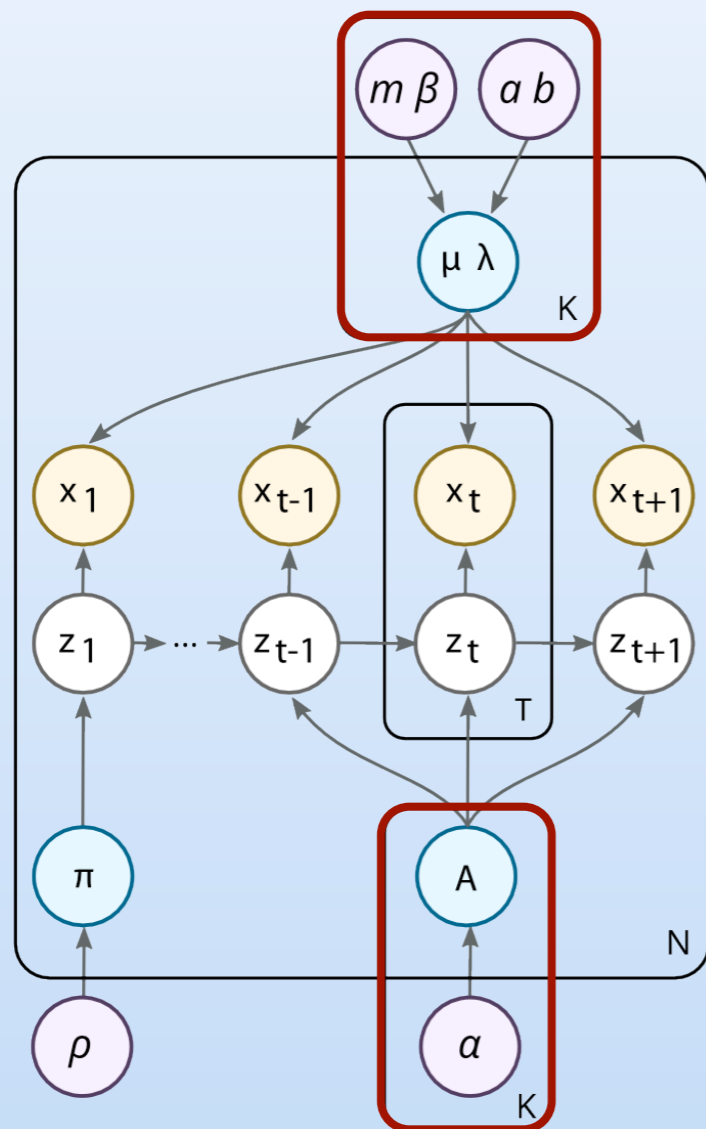
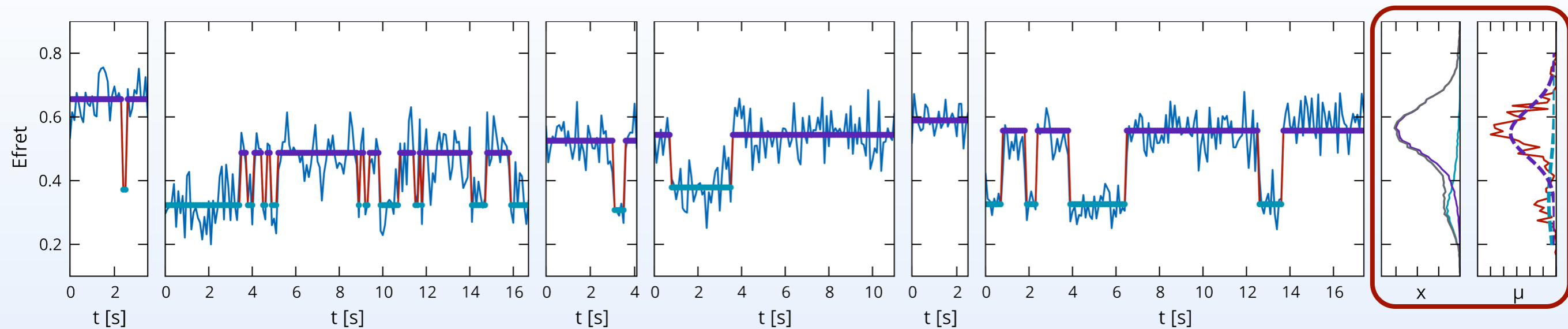


Single-molecule FRET studies of the Ribosome  
Ruben Gonzalez (Columbia)

# HMMs on multiple time series



# HMMs on multiple time series



## Hierarchical Coupling

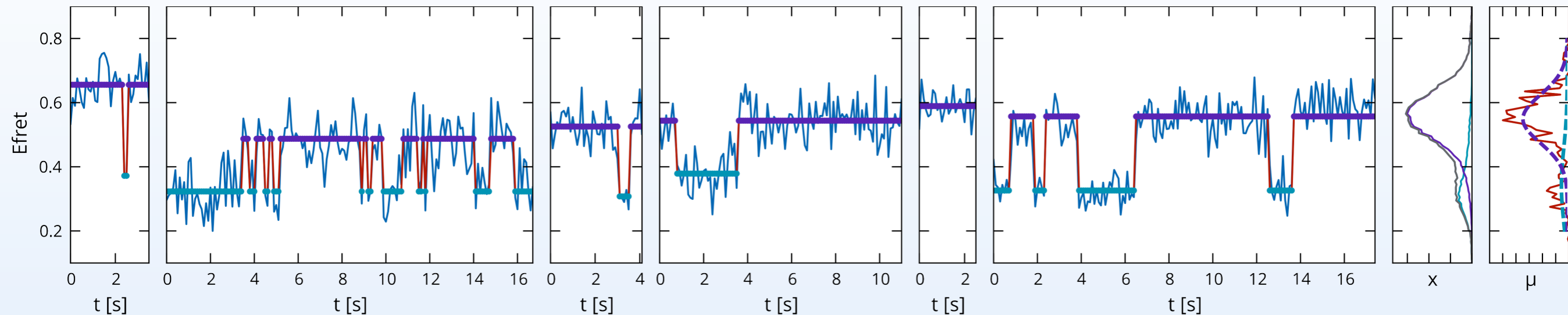
$$\mu_{n,k} \sim \text{Norm}(m_k, \beta_k \lambda_k)$$

$$\lambda_{n,k} \sim \text{Gamma}(a_k, b_k)$$

$$A_{n,k} \sim \text{Dir}(\alpha_k)$$

$$\pi_n \sim \text{Dir}(\rho)$$

# Hyperparameter Estimation



## Variational Empirical Bayes

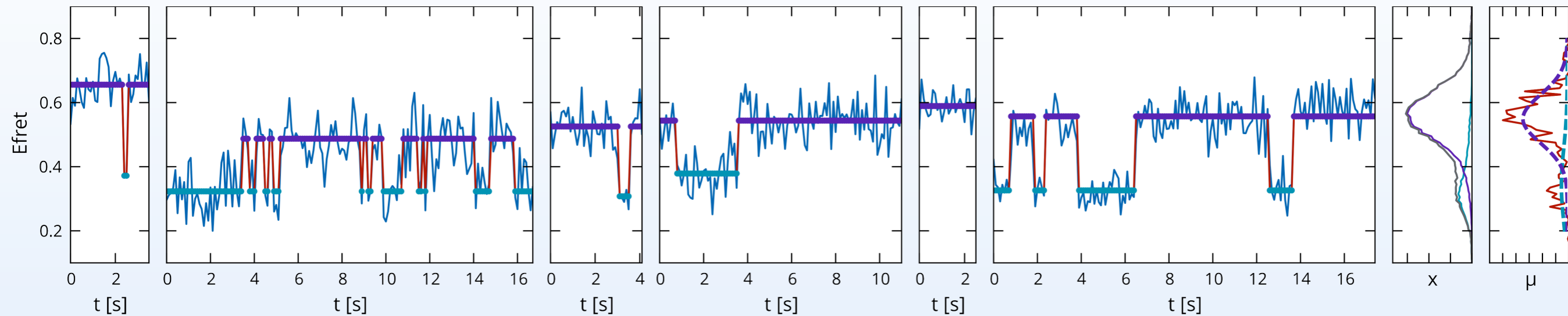
$$q(z_n) = \operatorname{argmin}_{q(z_n)} D_{\text{KL}}[q(z_n)q(\theta_n) \parallel p(z_n, \theta_n \mid x_n, \psi)]$$

$$q(\theta_n) = \operatorname{argmin}_{q(\theta_n)} D_{\text{KL}}[q(z_n)q(\theta_n) \parallel p(z_n, \theta_n \mid x_n, \psi)]$$

$$\psi = \operatorname{argmin}_{\psi} \sum_n D_{\text{KL}}[q(\theta_n) \parallel p(\theta_n \mid \psi)]$$



# Hyperparameter Estimation



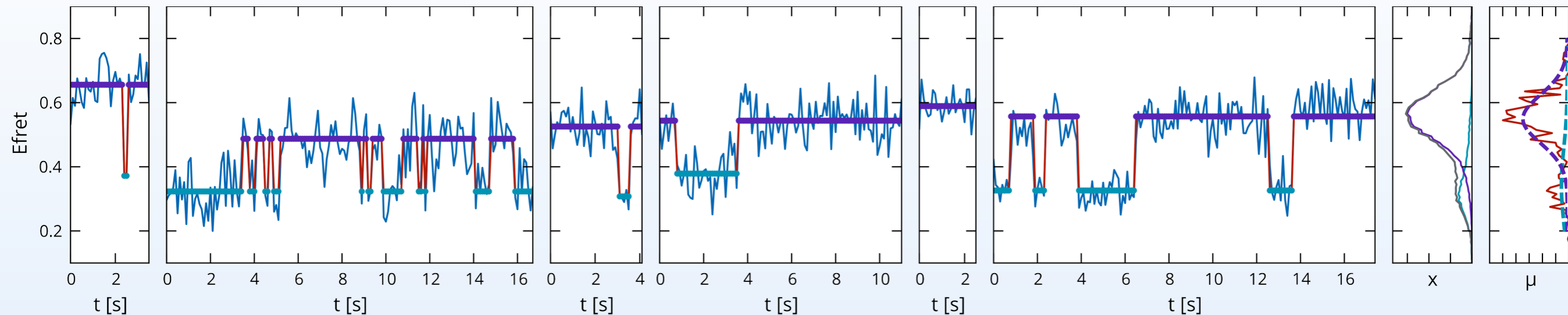
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# Hyperparameter Estimation



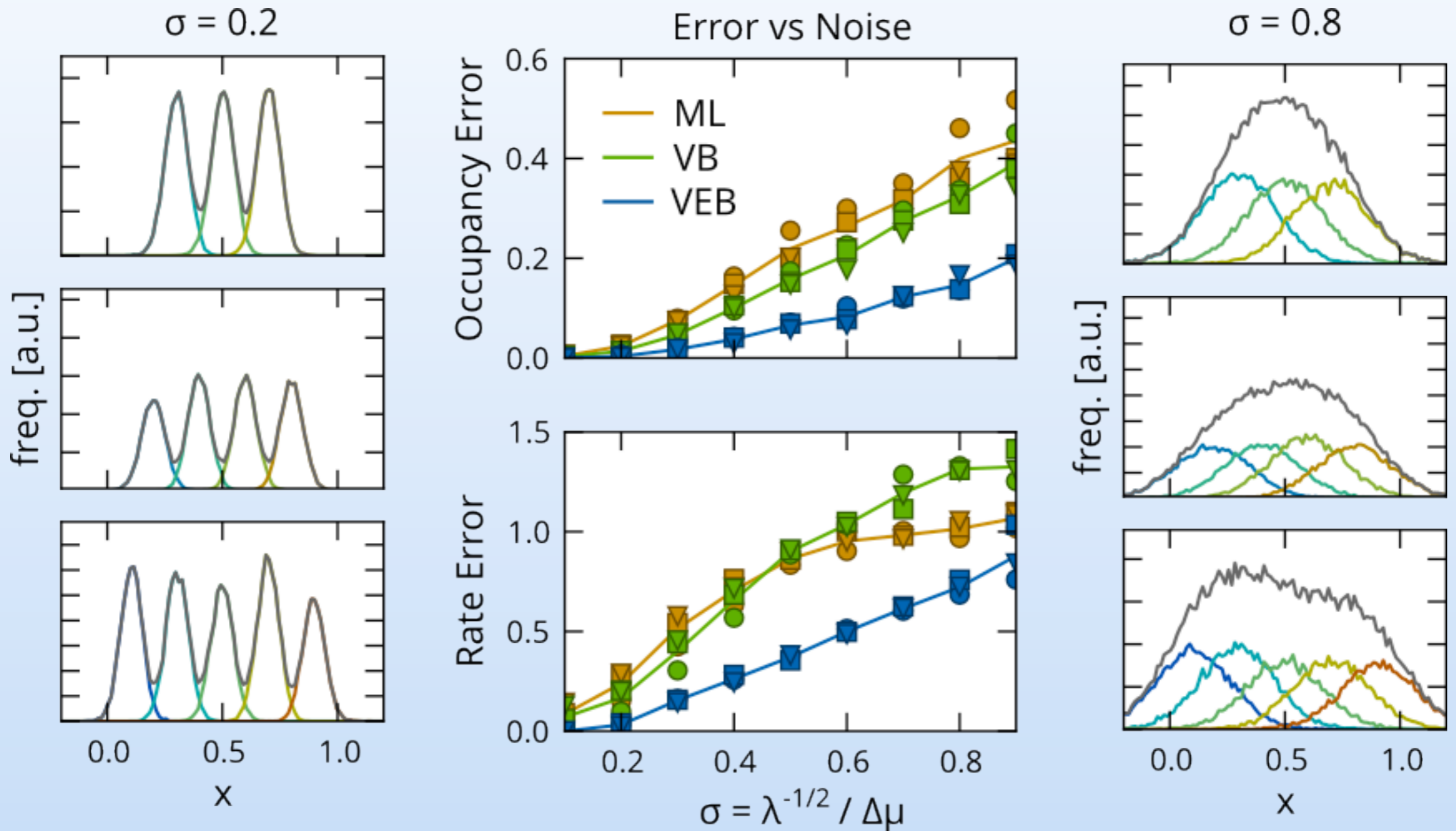
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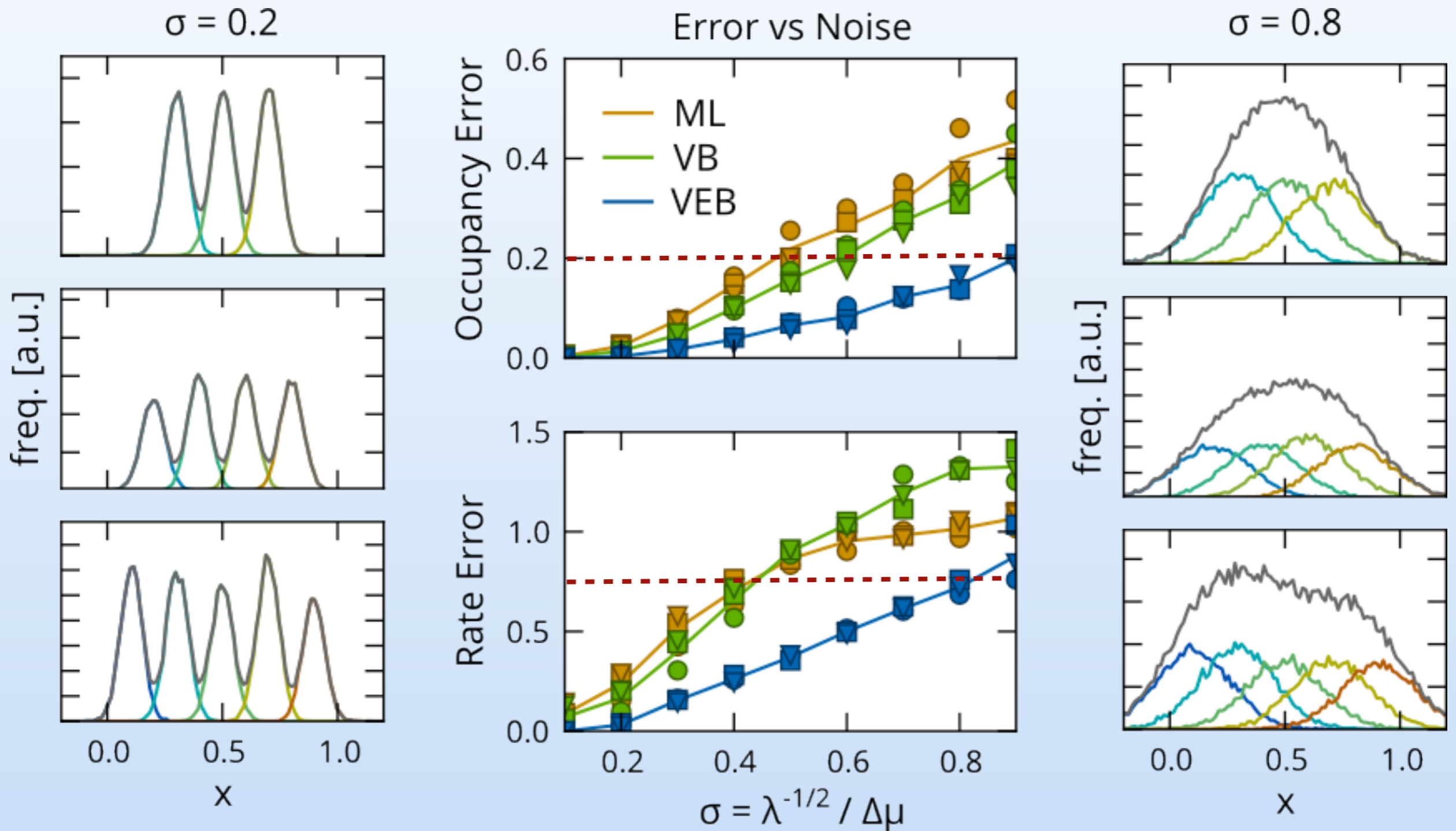
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# Transition Count Error vs Noise

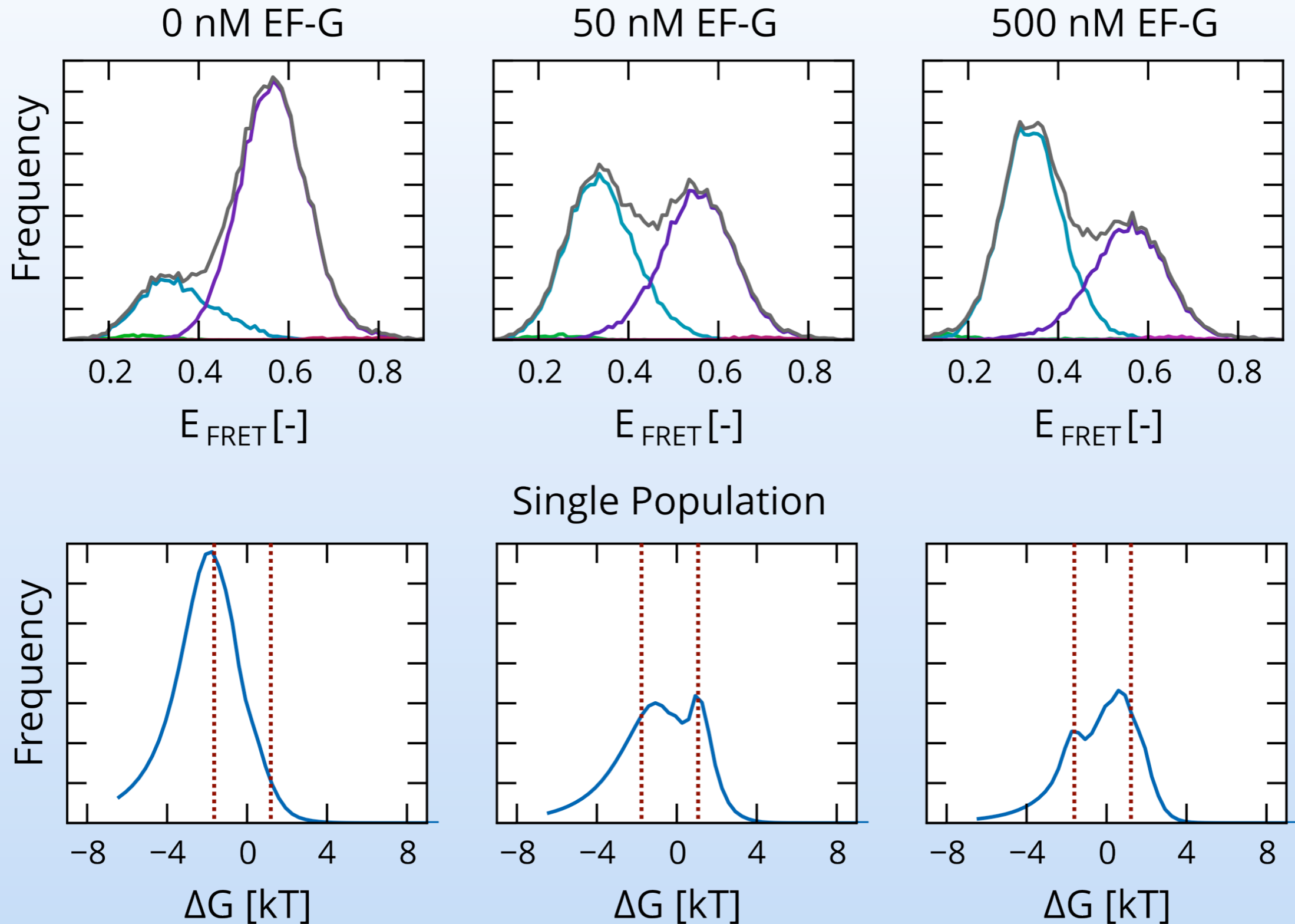


# Transition Count Error vs Noise



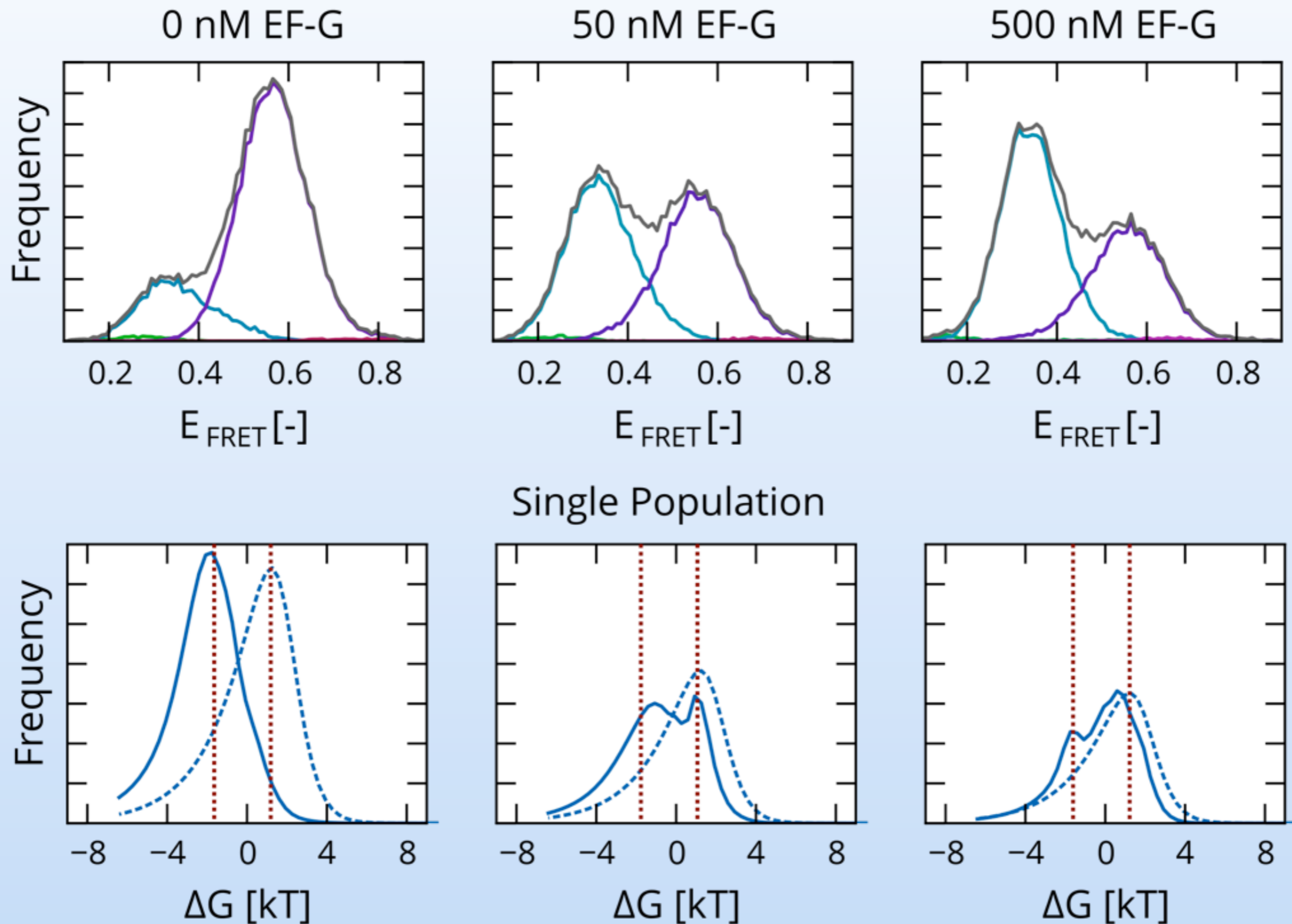
# Detecting Subpopulations

Fei, Bronson, Hofman, Srinivas, Wiggins, Gonzalez, PNAS, 2009



# Detecting Subpopulations

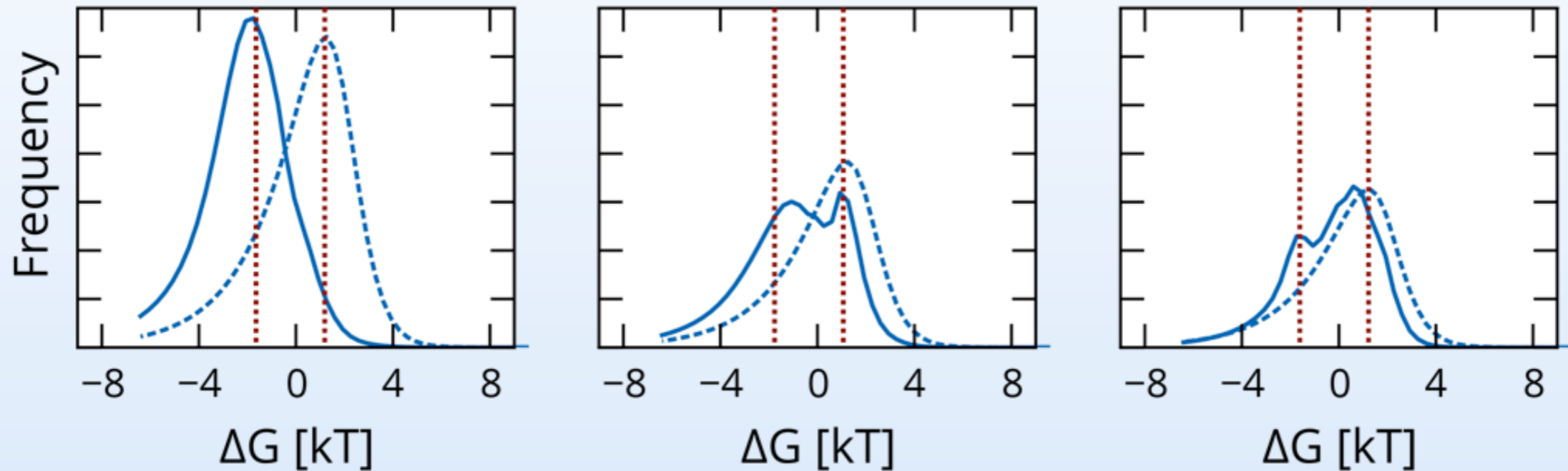
Fei, Bronson, Hofman, Srinivas, Wiggins, Gonzalez, PNAS, 2009



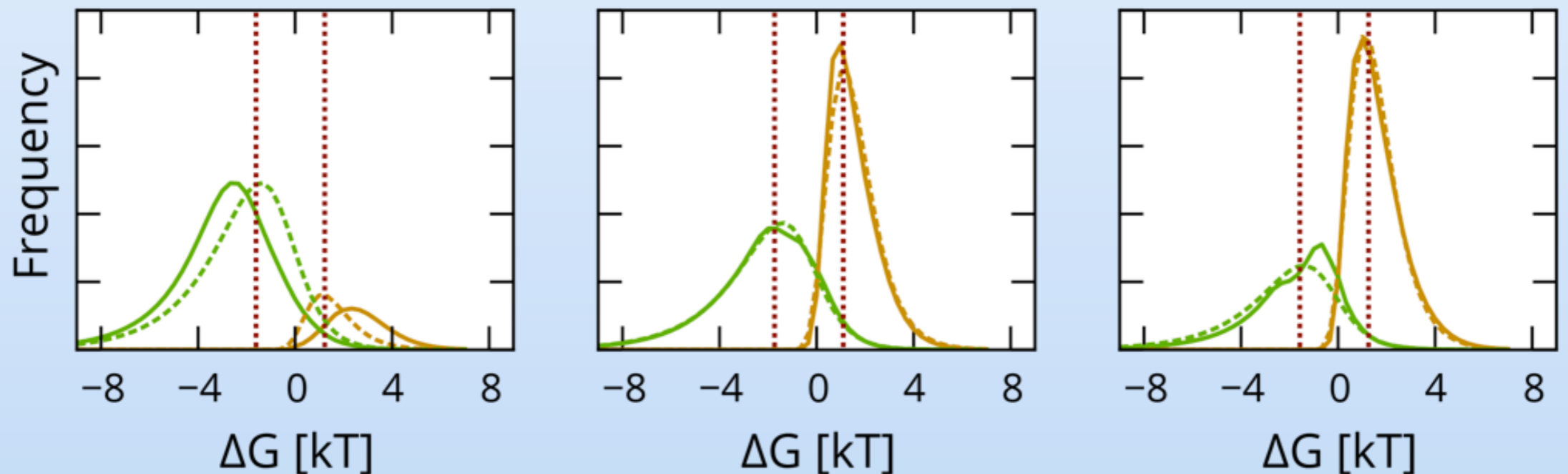
# Detecting Subpopulations

Fei, Bronson, Hofman, Srinivas, Wiggins, Gonzalez, PNAS, 2009

Single Population



Two Populations: EF-G bound / Unbound



# Co-conspirators

Columbia

Oxford



Jan-Willem  
van de Meent



Chris  
Wiggins



Ruben  
Gonzalez



Frank  
Wood

Poster 670

<http://ebfret.github.io>